



煤矿灾害动力学与控制全国重点实验室

State key laboratory of coal mine disaster dynamics and control



SKL-CMD



重庆大学  
CHONGQING UNIVERSITY



MSTP 2025, Sep. 26-28, 2025, Hefei, China

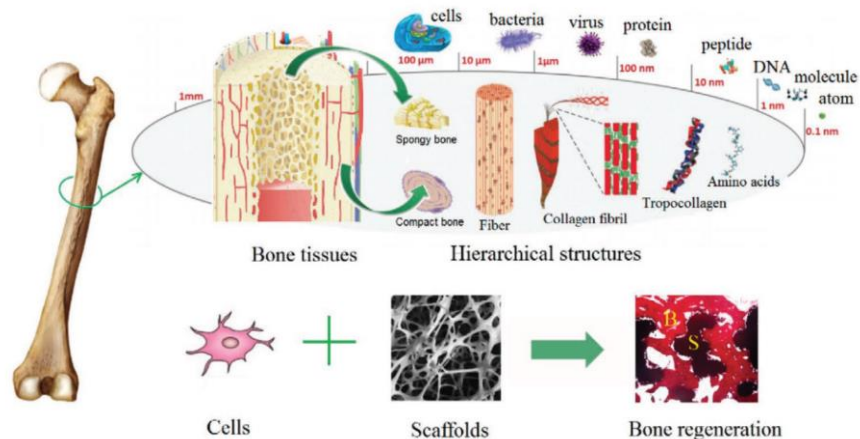
# Flow and Transport in Multiscale Pore Structures: Model Development and Simulations

Chao-Zhong Qin, Bowen Shi, Han Jiang, Xingyuan Zhao (Chongqing University, China)

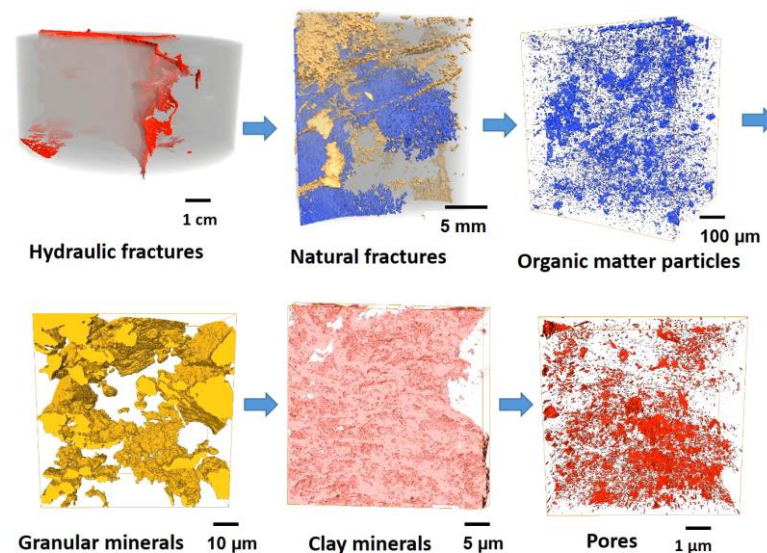
Bo Guo (University of Arizona, USA)

- 1. Multiscale porous materials and research challenges**
- 2. Two hybrid numerical models for multiscale digital rocks**
- 3. Predictions of single-phase and two-phase flow parameters**
- 4. Conclusions and outlook**

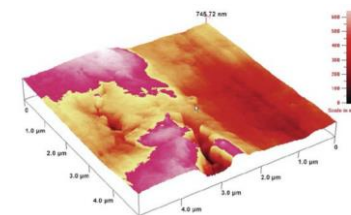
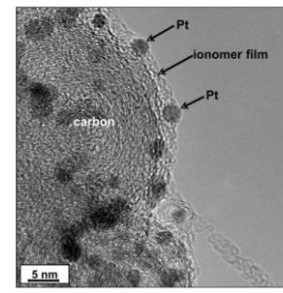
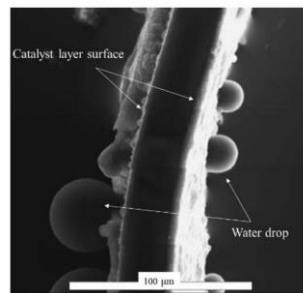
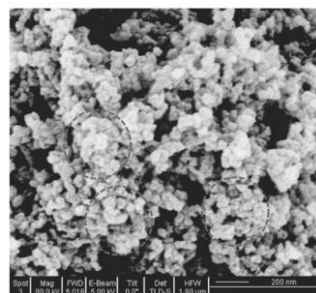
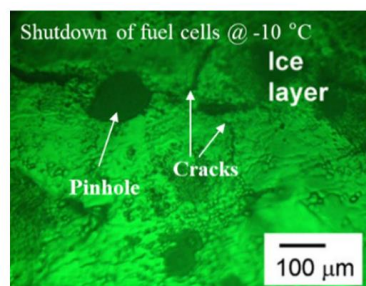
# Multiscale porous materials across different applications



Hierarchical pore structure of bone tissue (*Adv. Funct. Mater.* 2021, 31, 2010609)



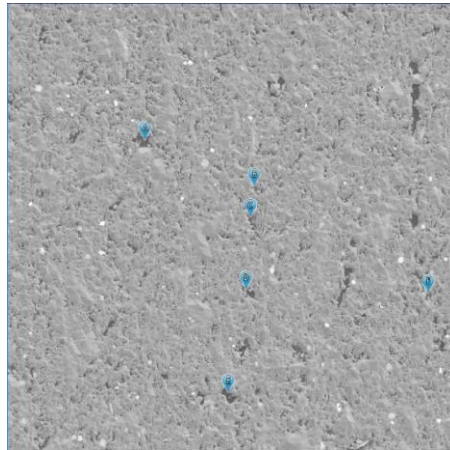
Hierarchical pore structures of shale



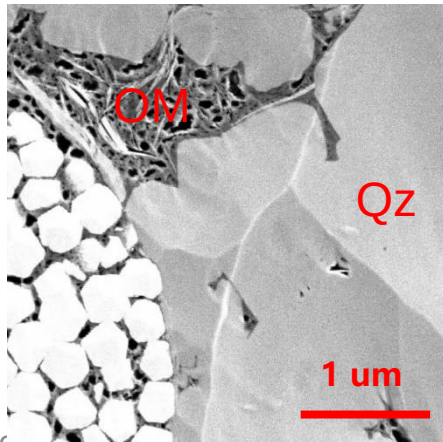
Hierarchical pore structure of catalysts (*Electrochem. Energ. Rev.* 2023, 6, 13)

# Research challenges for flow and transport

- ❑ How do multiscale pore structures regulate flow and transport?
- ❑ The role of wettability in flow and transport, and how to control wettability?

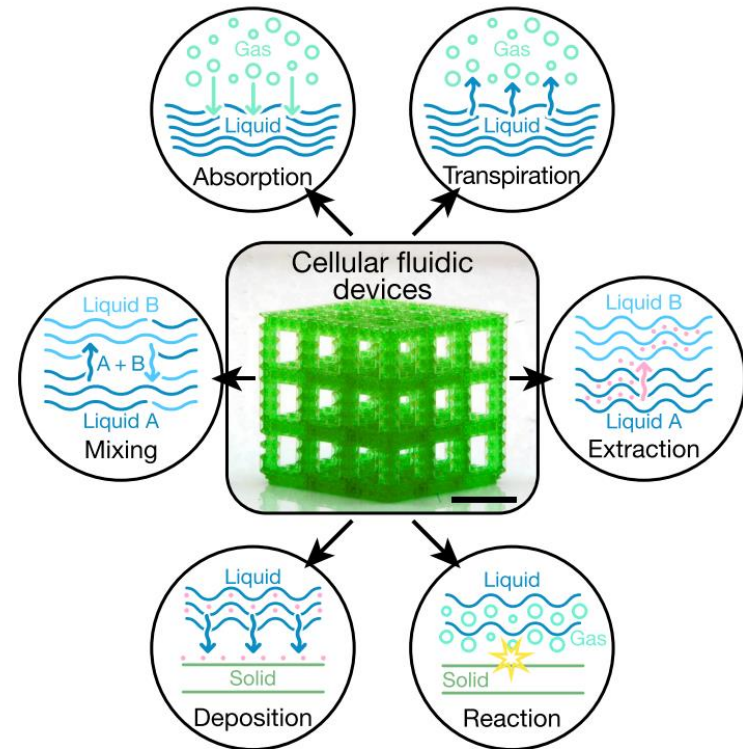


MAPS of shale



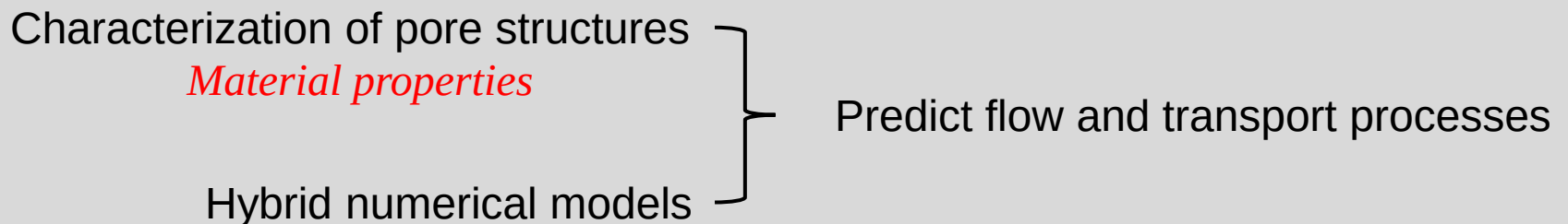
10/10/2023

Combine wettability and multiscale pore structures?



Nature, 2021

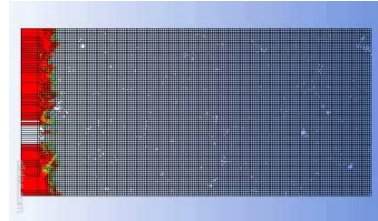
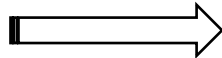
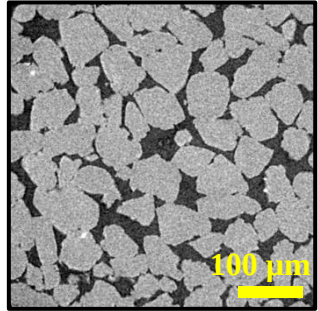
1. Multiscale porous materials and research challenges
2. Two hybrid numerical models for multiscale digital rocks
3. Predictions of single-phase and two-phase flow parameters
4. Conclusions and outlook





# Digital Core Analysis (DCA) – multiscale pore structures

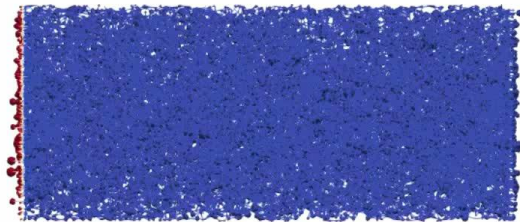
Nubian sandstone



Time: 0.000000

VOF modeling of water imbibition,  
 $100 \times 100 \times 200$  image

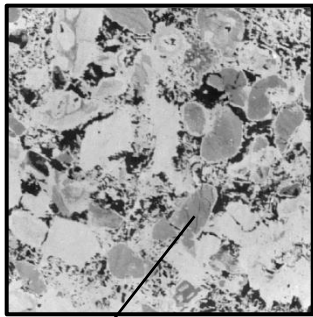
(Qin et al., AWR, 2021)



$900 \times 900$   
 $\times 2000$   
image

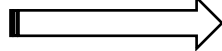
Dynamic pore-network  
modeling of cocurrent  
spontaneous imbibition

Estailades carbonate



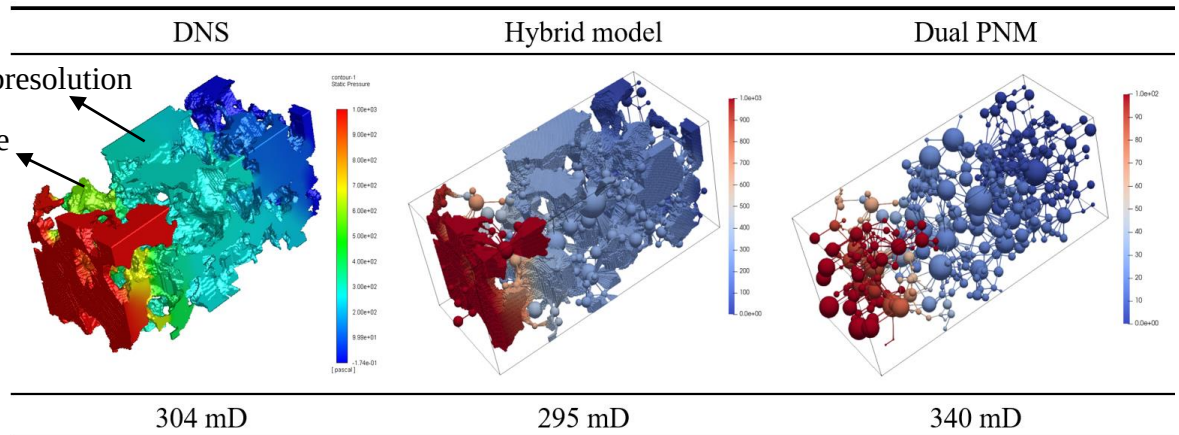
Subresolution  
microporosity

10/8/2025



subresolution

Macropore

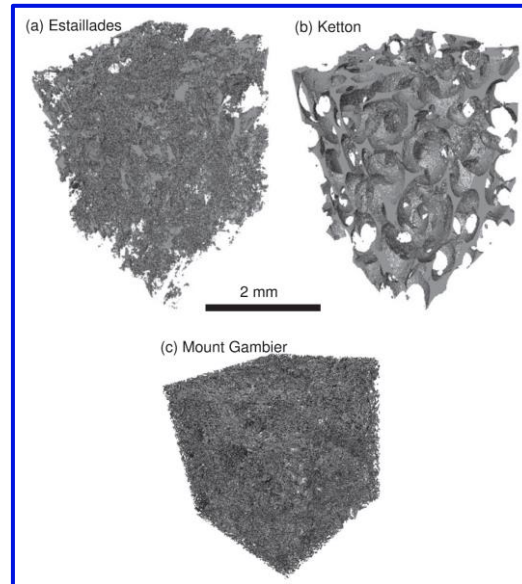


(Qin et al., TiPM, 2025)

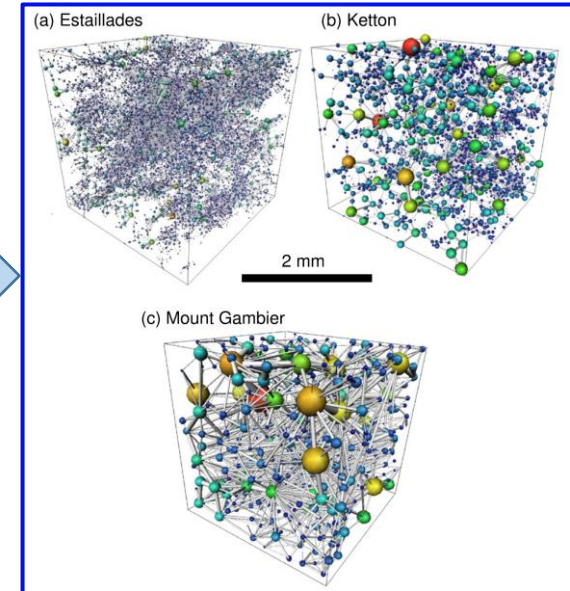
# Pore-network models – between DNS and continuum

## Flow and transport

- ❑ Quasi-static or dynamic two-phase flow
- ❑ Reactive flow and transport
- ❑ Non-Newtonian fluid flow
- ❑ Mineral precipitation and dissolution
- ❑ And so on.



Extract pore networks



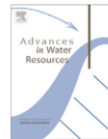
Advances in Water Resources 51 (2013) 197–216



Contents lists available at SciVerse ScienceDirect

Advances in Water Resources

journal homepage: [www.elsevier.com/locate/advwatres](http://www.elsevier.com/locate/advwatres)



## Pore-scale imaging and modelling

Martin J. Blunt<sup>a,\*</sup>, Branko Bijeljic<sup>a</sup>, Hu Dong<sup>b</sup>, Oussama Gharbi<sup>c</sup>,  
Adriana Paluszny<sup>a</sup>, Christopher Pentland<sup>a</sup>

<sup>a</sup> Department of Earth Science and Engineering, Imperial College, London SW7 2AZ, UK

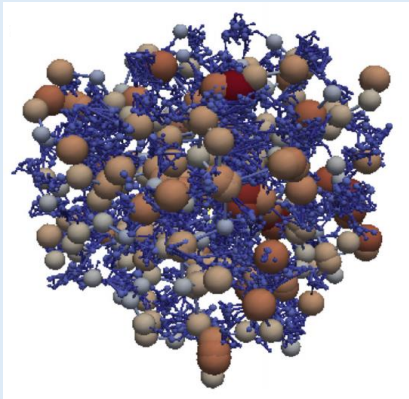
<sup>b</sup> iRock Technologies, Suite 1103, Tower A, Oriental Media Center, No. 4 Guanghua Road, Chaoyang District, Beijing 100020, China

<sup>c</sup> Department of Petroleum Engineering, Curtin University, 6151 Perth, Australia

it is difficult to resolve thin wetting layers that control many processes in two and three-phase flow [1,7,8]; this limitation is discussed further at the end of the paper. In the literature to date, the most computationally efficient and successful predictions of multiphase flow come from network modelling, described below.

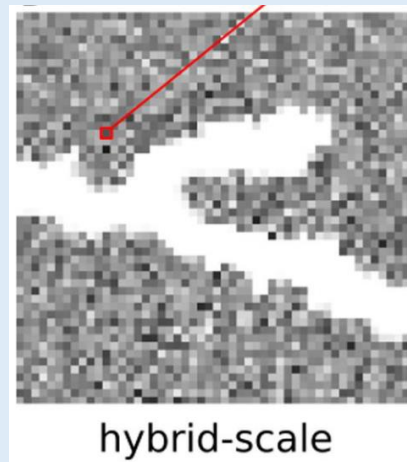
# Numerical models for multiscale porous media

Dual-pore-network  
model (DPNM)



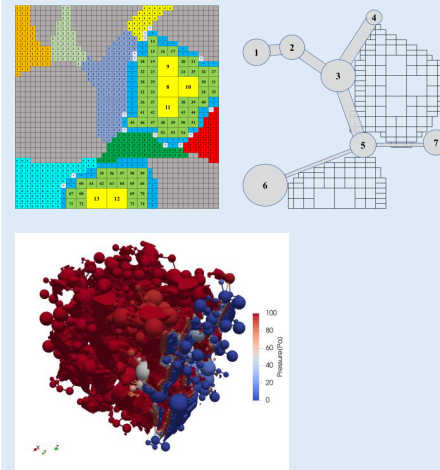
Mehmani, 2014

Micro-continuum  
model (MCM)



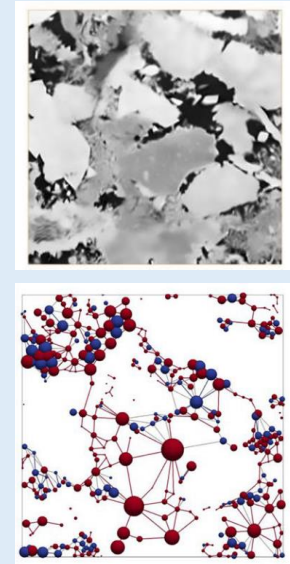
Soulaine, 2023

Pore-network-  
continuum model  
(PNCM)



Qin, 2024

Multiscale pore-  
network model  
(MPNM)



- ❑ The MPNM is most efficient, but **its verification is missing**.
- ❑ The PNCM can **balance efficiency and accuracy**.



# The multiscale pore-network model (MPNM)

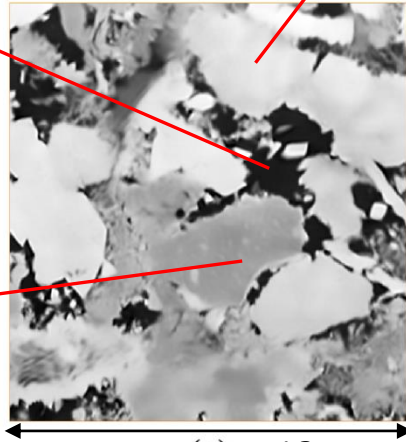
Macropores

Solid

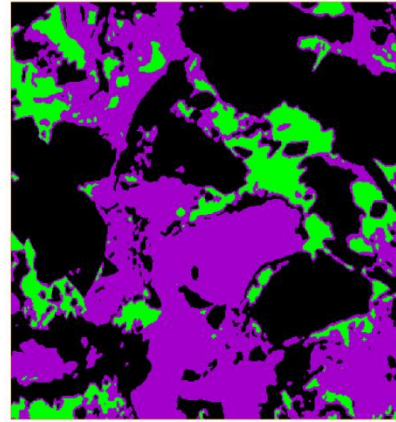
Segmentation

Watersheds

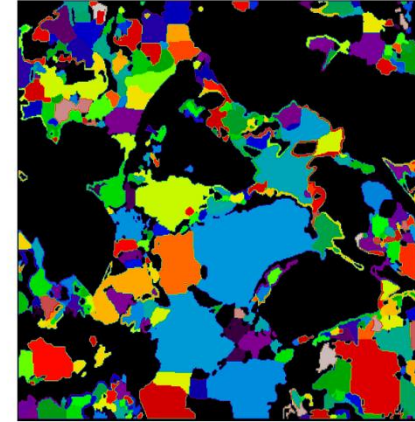
Microporosity



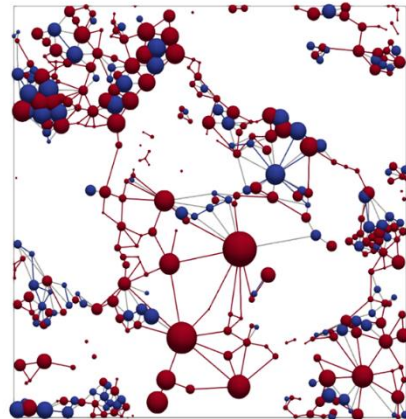
(a) 1.2 mm



(b)

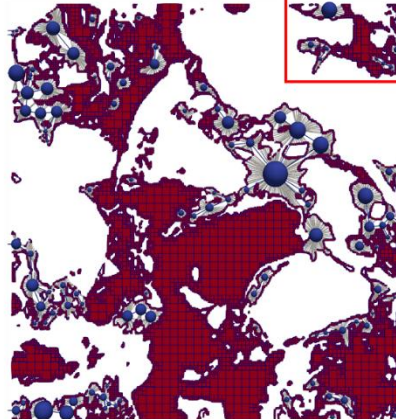


(c)

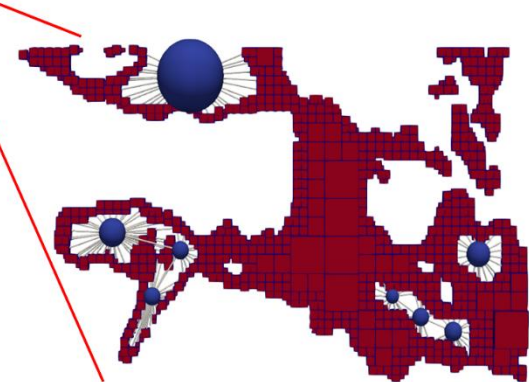


(d)

**Blue:** resolved pores  
**Red:** subresolution elements



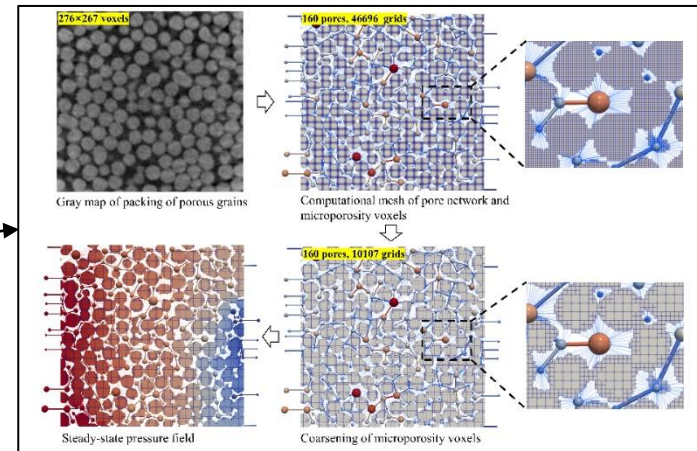
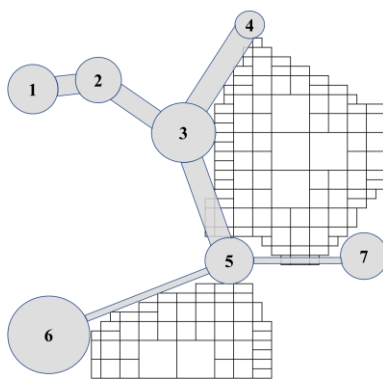
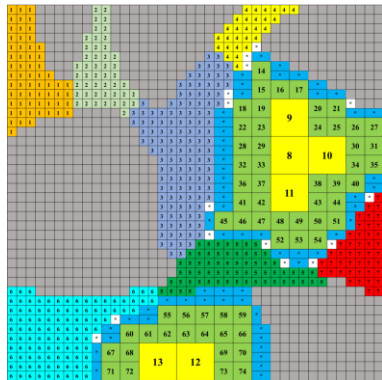
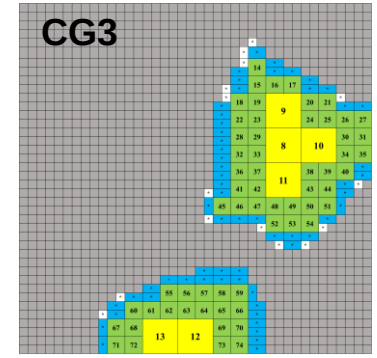
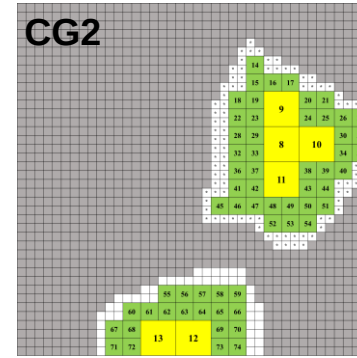
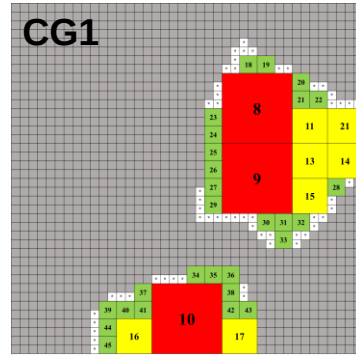
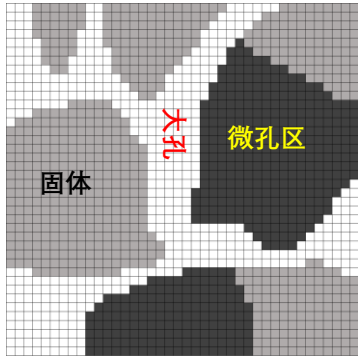
(e)



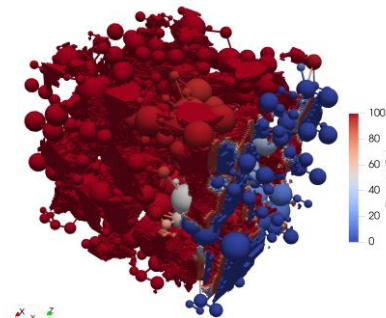
(f)

1. Modeling of permeability and formation factor of carbonate digital rocks: dual-pore-network and pore-network-continuum models. Transport in Porous Media, 152:37, 2025
2. Modeling of flow and transport in multiscale digital rocks aided by grid coarsening of microporous domains. Journal of Hydrology, 633:131003, 2024

# Pore-network-continuum model – coarsening algorithm



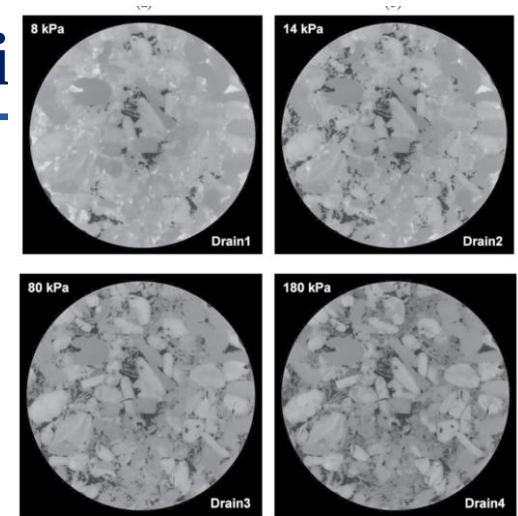
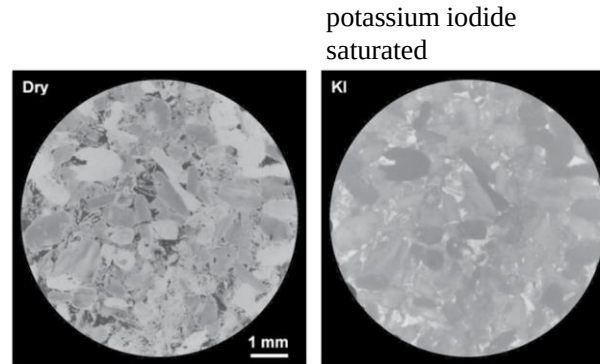
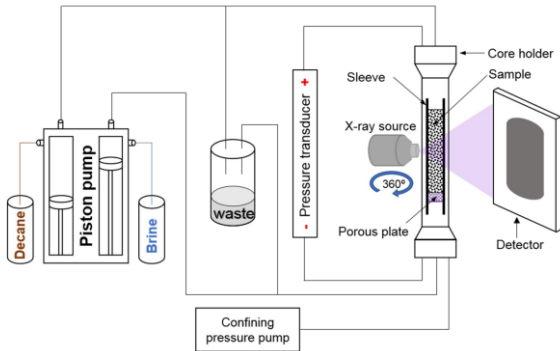
Packing of porous particles



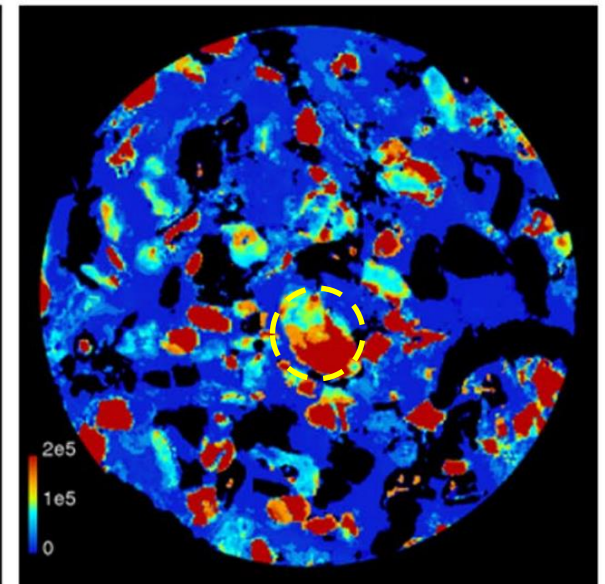
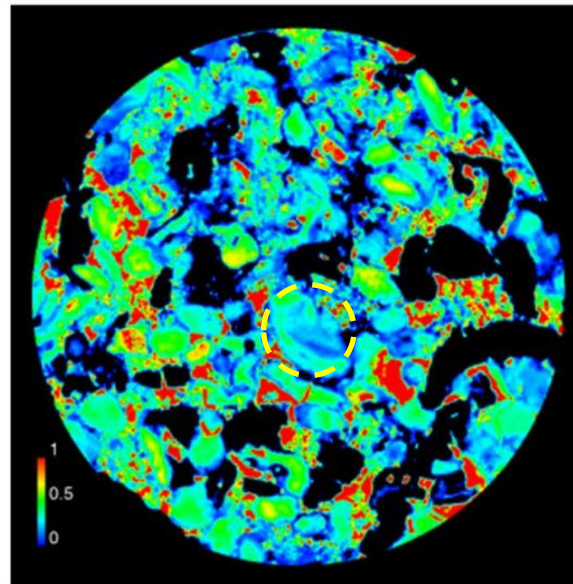
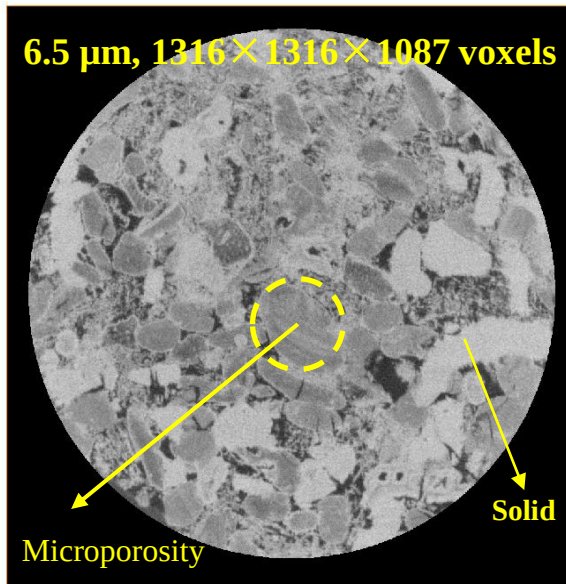
Depressurization process



# Characterization of ES6.5 microporosi



(Wang et al., WRR, 2022)



CT grey-scale map

Porosity map

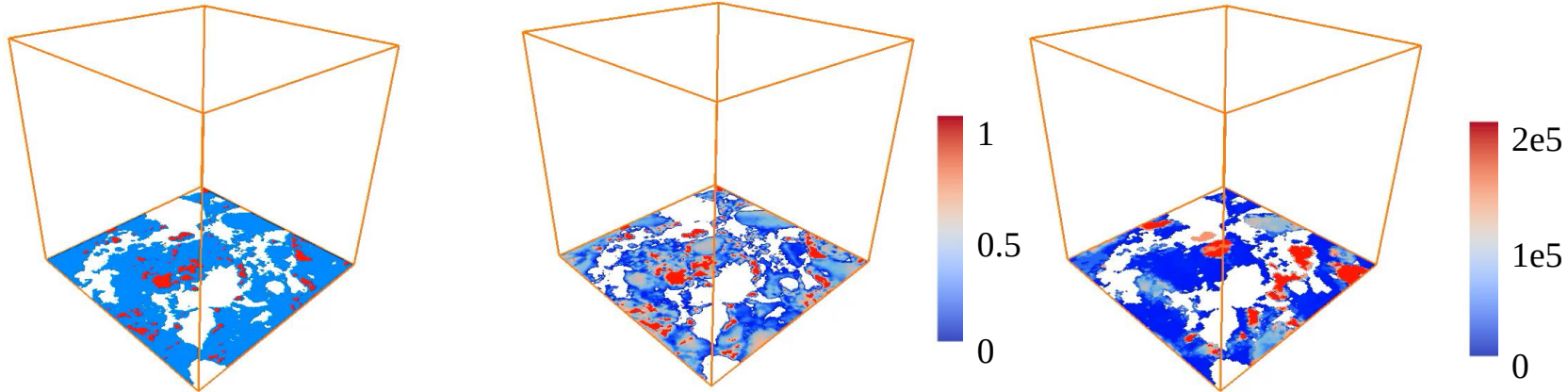
Entry pressure map

10/8/2025

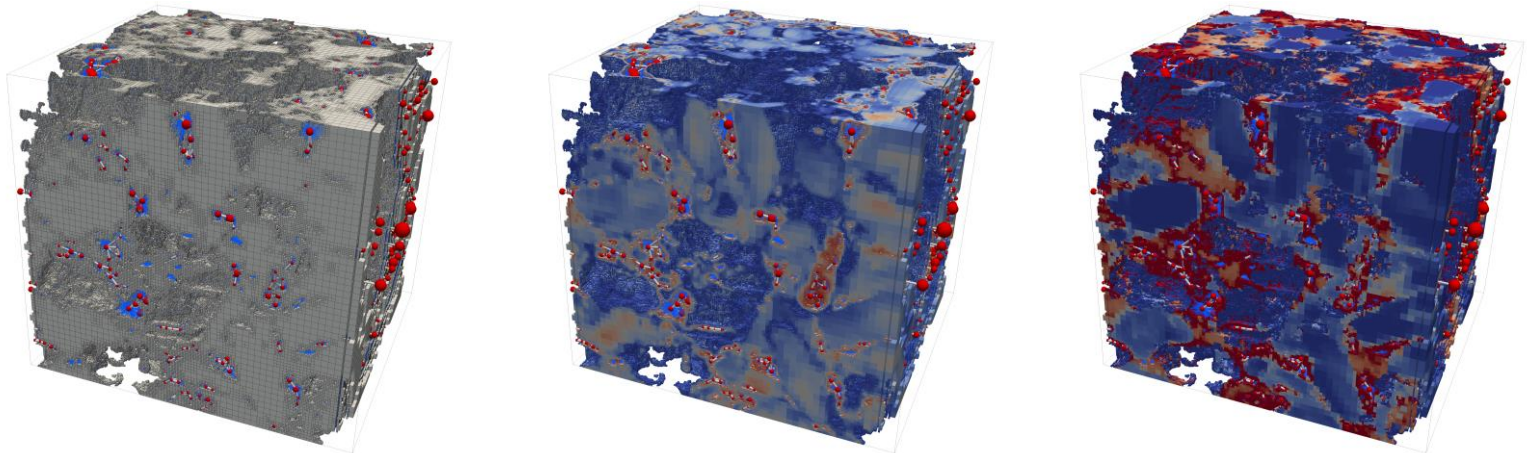
# Estailades carbonate rock: pore structures and mesh

<https://www.digitalrockportal.org/>

400<sup>3</sup>的测试岩心



Computational mesh for the PNCM modeling

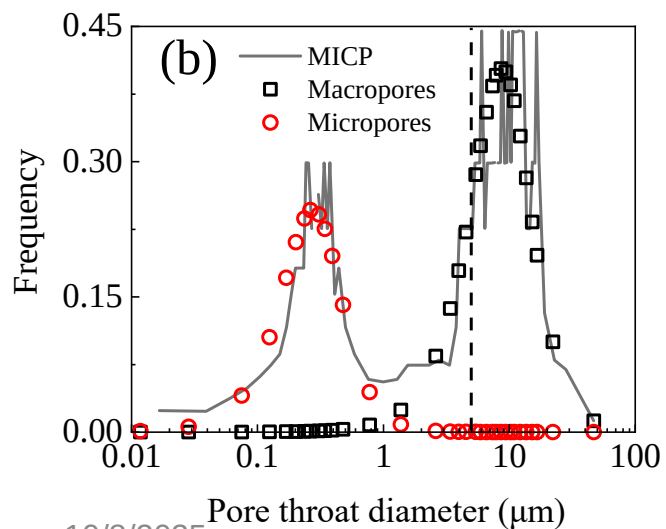
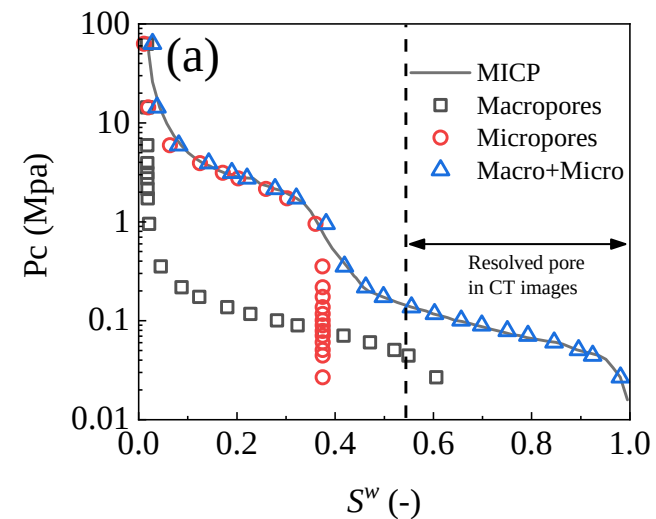




- 1. Introduction of multiscale pore-network model**
- 2. Predictions of absolute permeability and formation factor**
- 3. Predictions of capillary pressure and relative permeability**
- 4. Conclusions and outlook**

# The importance of $p^c$ and $k_r$

$p^c$  can infer pore-size distributions of porous media

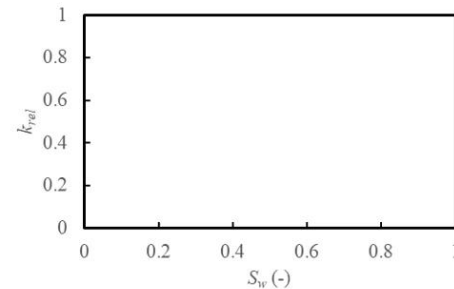
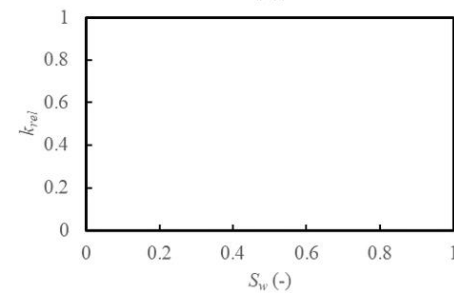
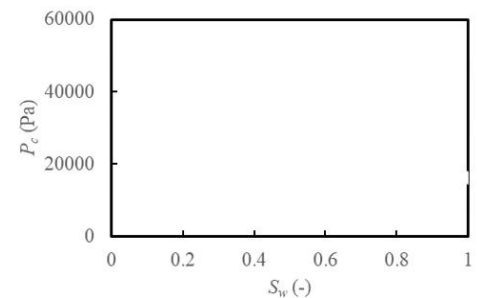


Wetting reservoir

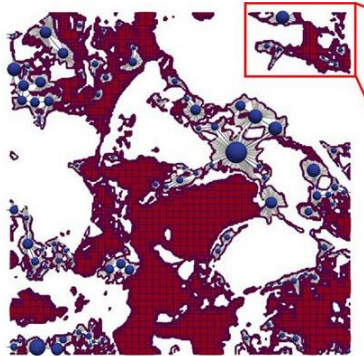
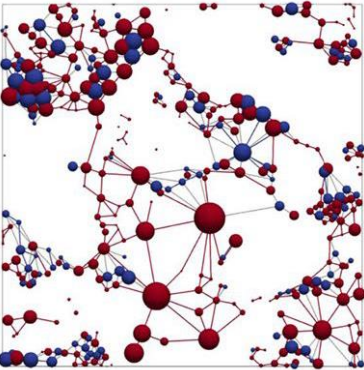
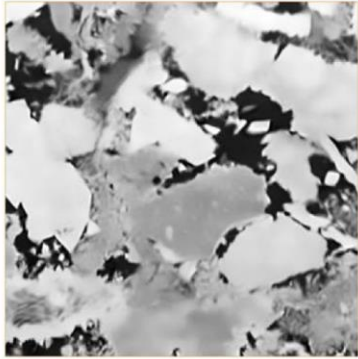
Drainage



Non-wetting reservoir



# The average operation of pore sizes of microporosity in MPNM



10/8/2025

① Average based on sphere-assumption

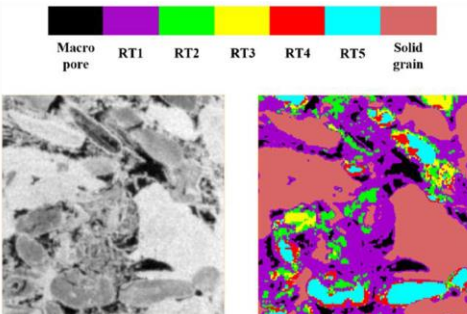
$$\bar{r}_i = \left( \frac{3}{4\pi} \frac{\sum_{k=1}^{N_i} V_k \varepsilon_k}{\sum_{k=1}^{N_i} M_k} \right)^{1/3}$$

$$M_k = V_k \varepsilon_k / (4\pi r_k^3 / 3)$$

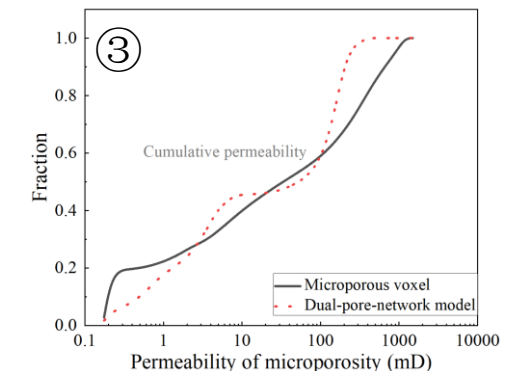
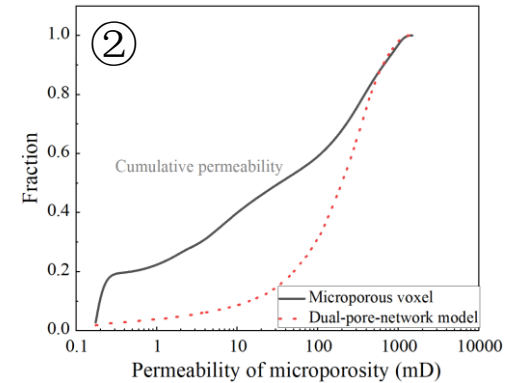
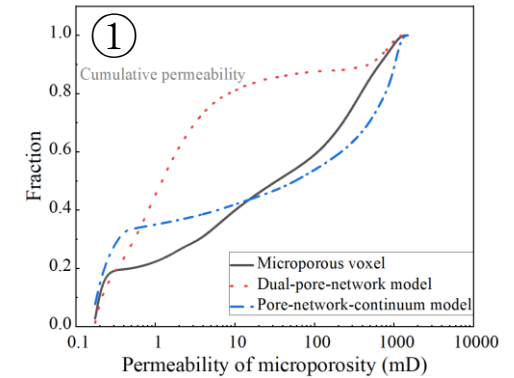
② Average based on voxel-counting

$$\bar{r}_j = \frac{\sum_{k=1}^{N_i} \sum r}{N_i}$$

③ Entry-pressure-based sub-rock typing (Wang et al., 2022)

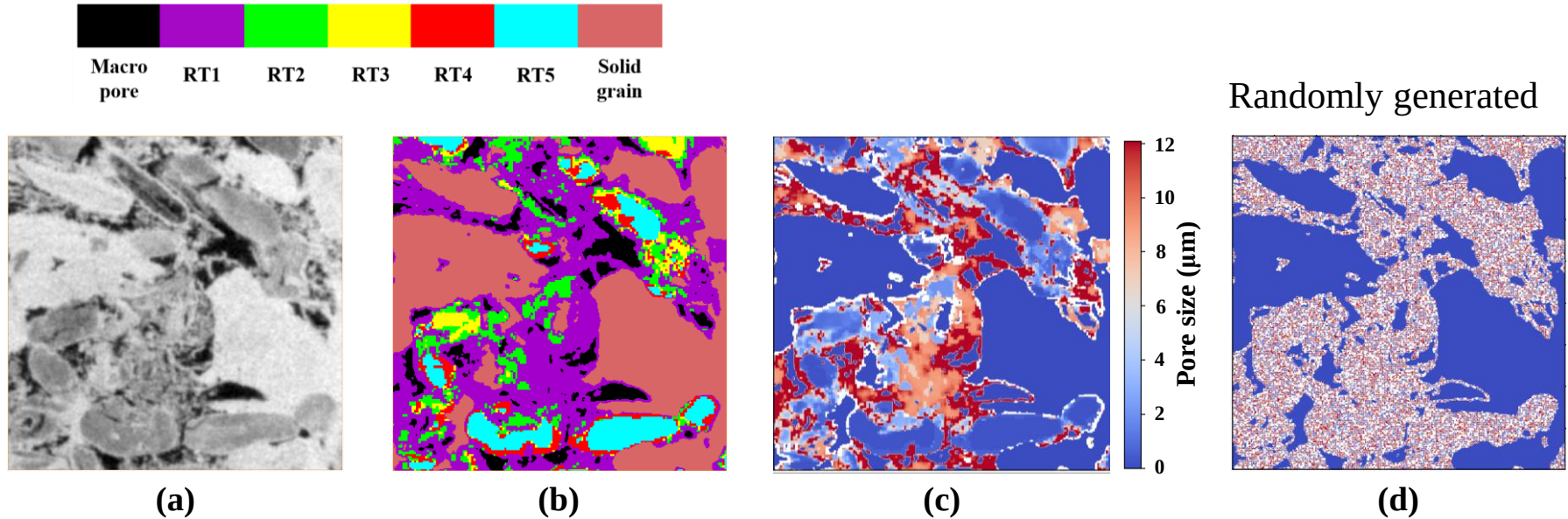


Estimation of microporosity permeability distribution



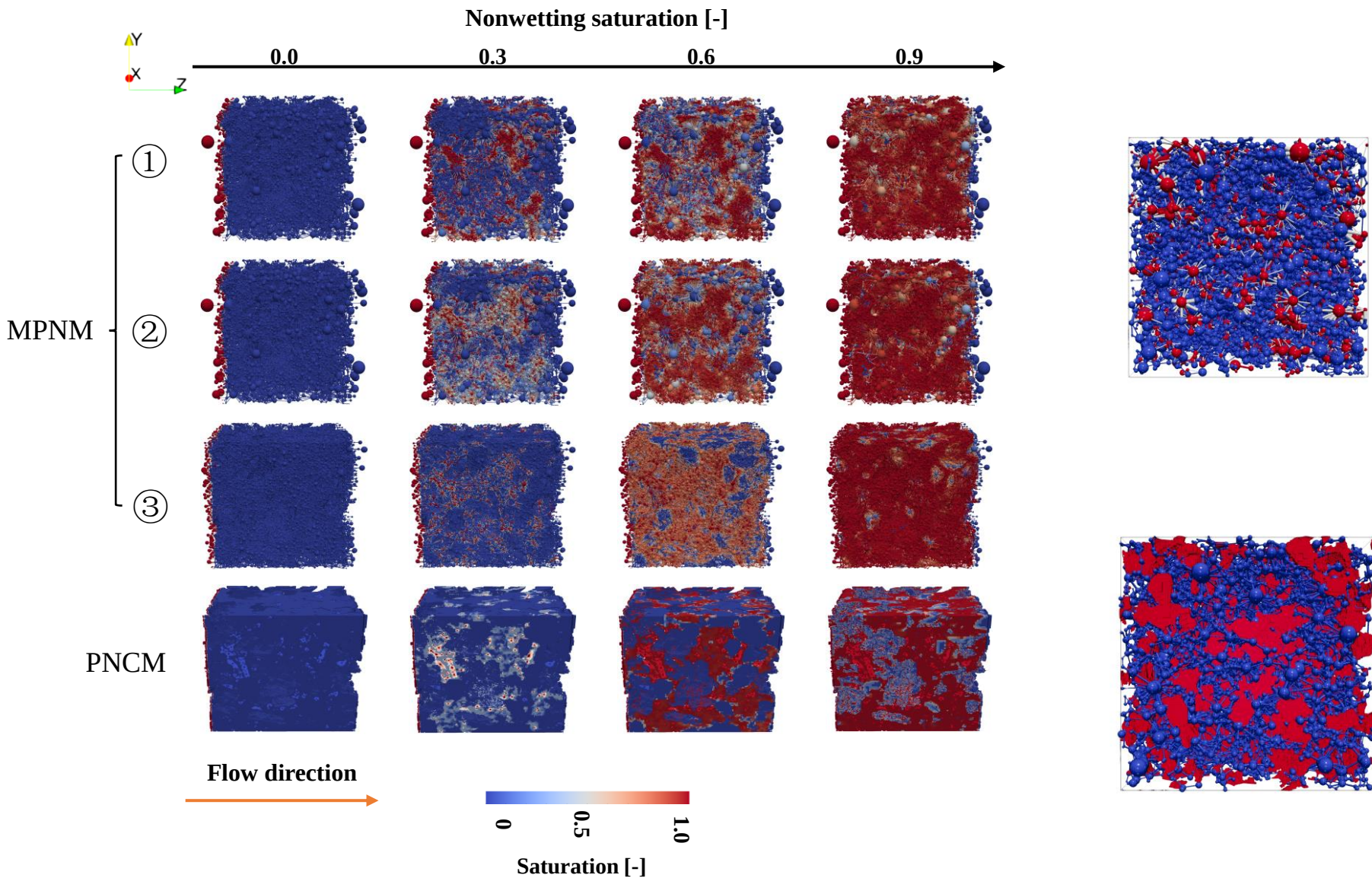


# Why do we need the sub-rock typing?

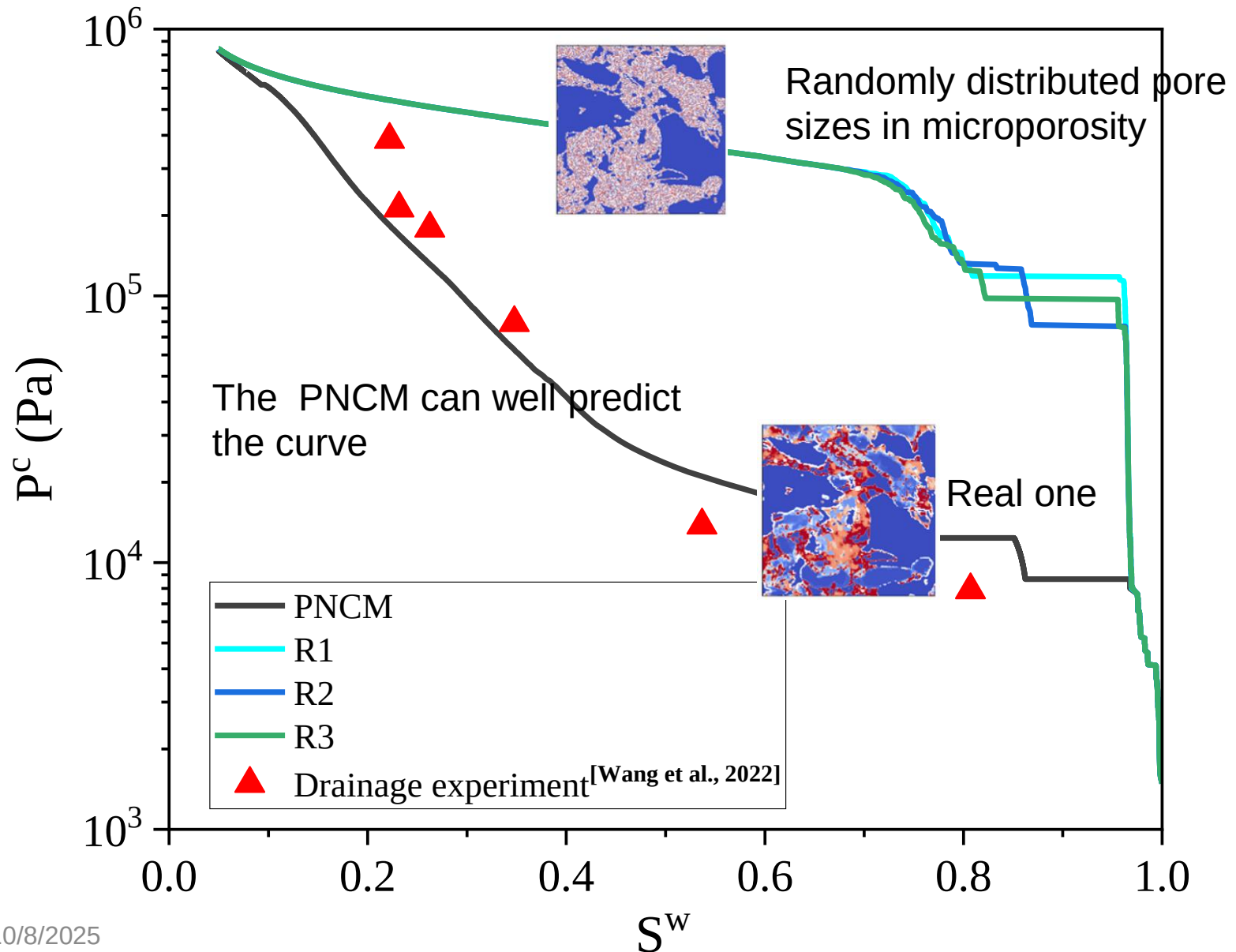


- ❑ The sub-rock typing helps with the prediction, but the CT-based characterization is **costly and time-consuming** !
- ❑ If only the MICP data is used, **the correlation of pore sizes** should be taken into account.

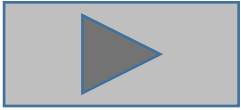
# Review the model setup (400<sup>3</sup> sub-volume of ES6.5)



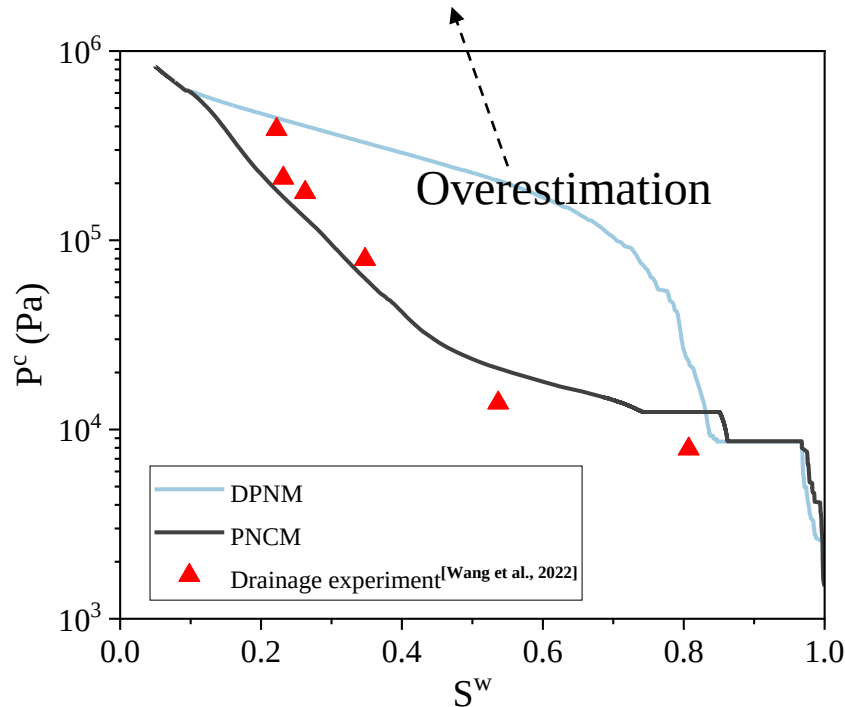
# Capillary pressure curve predicted by the PNCM



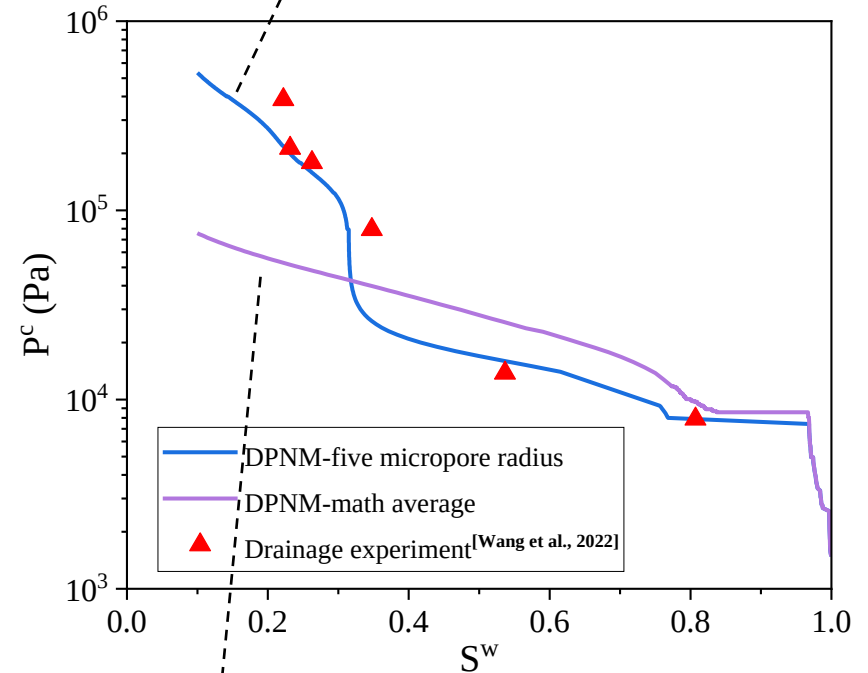
# Capillary pressure curve by the MPNM



① Average based on sphere-assumption



③ Entry-pressure-based sub-rock typing (Wang et al., 2022)

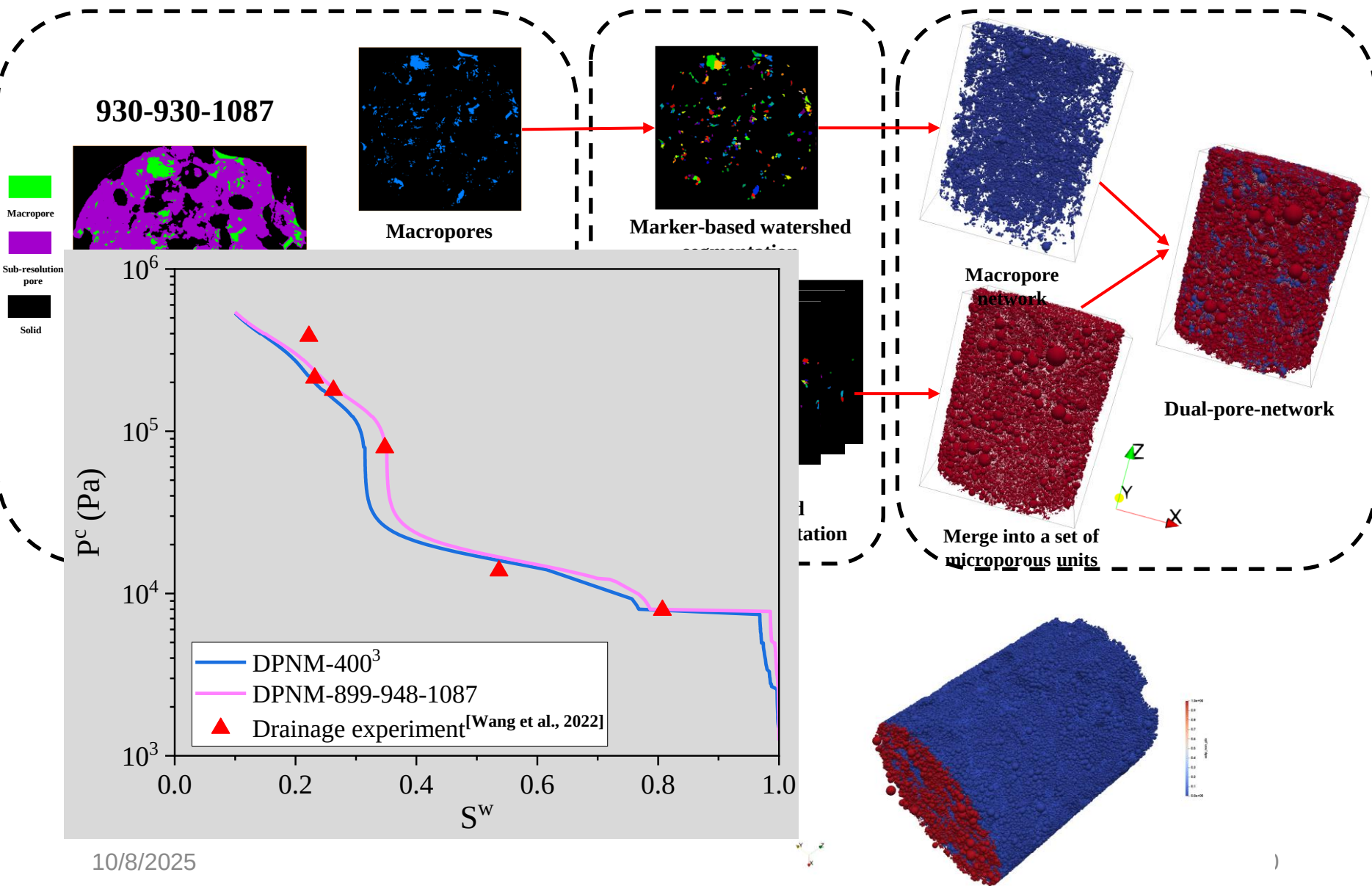


② Average based on voxel-counting

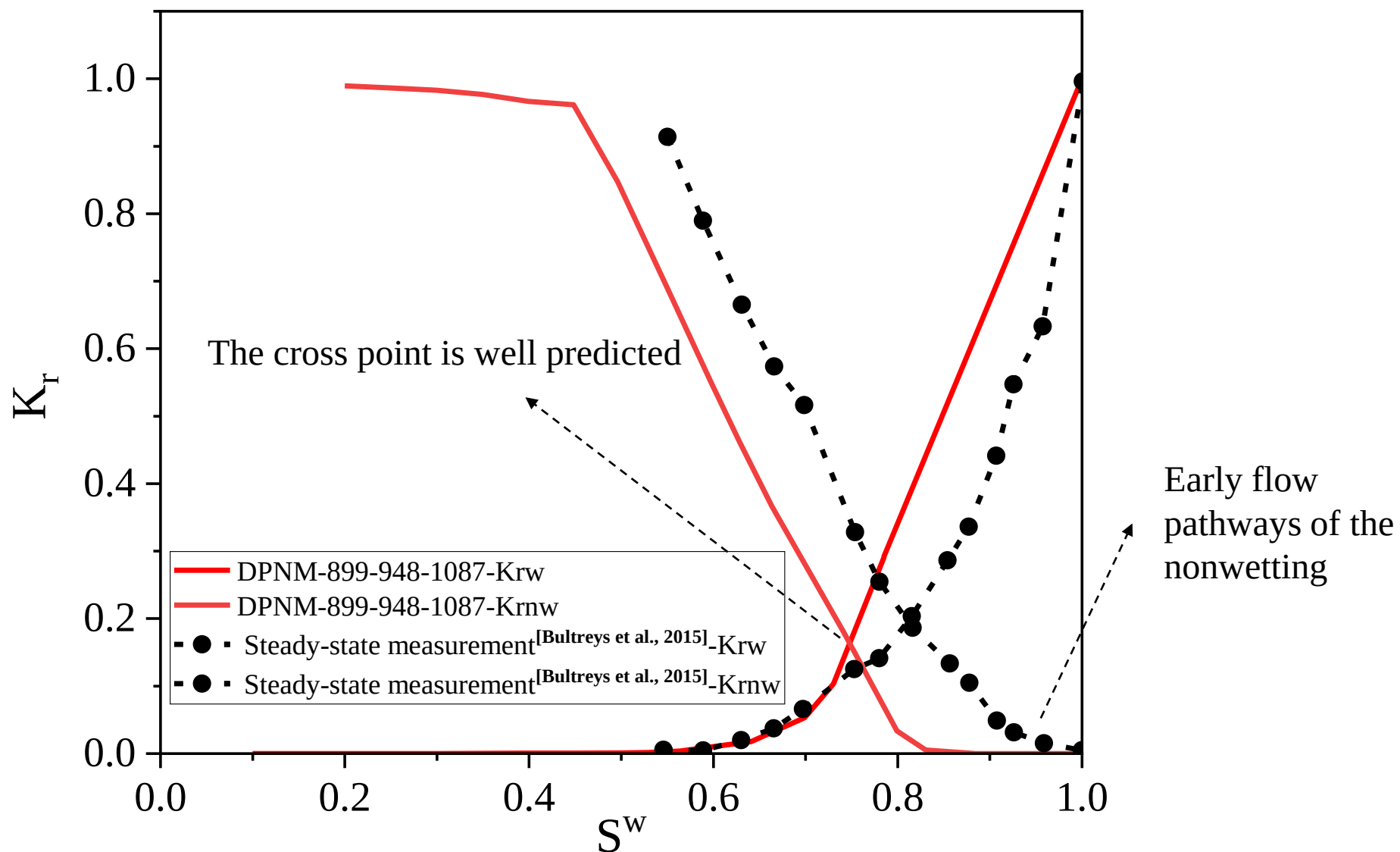
- ❑ The **sub-rock typing** is essential to the efficient multiscale pore-network model.
- ❑  $400^3$  size **is adequate to** the prediction of capillary pressure curve.



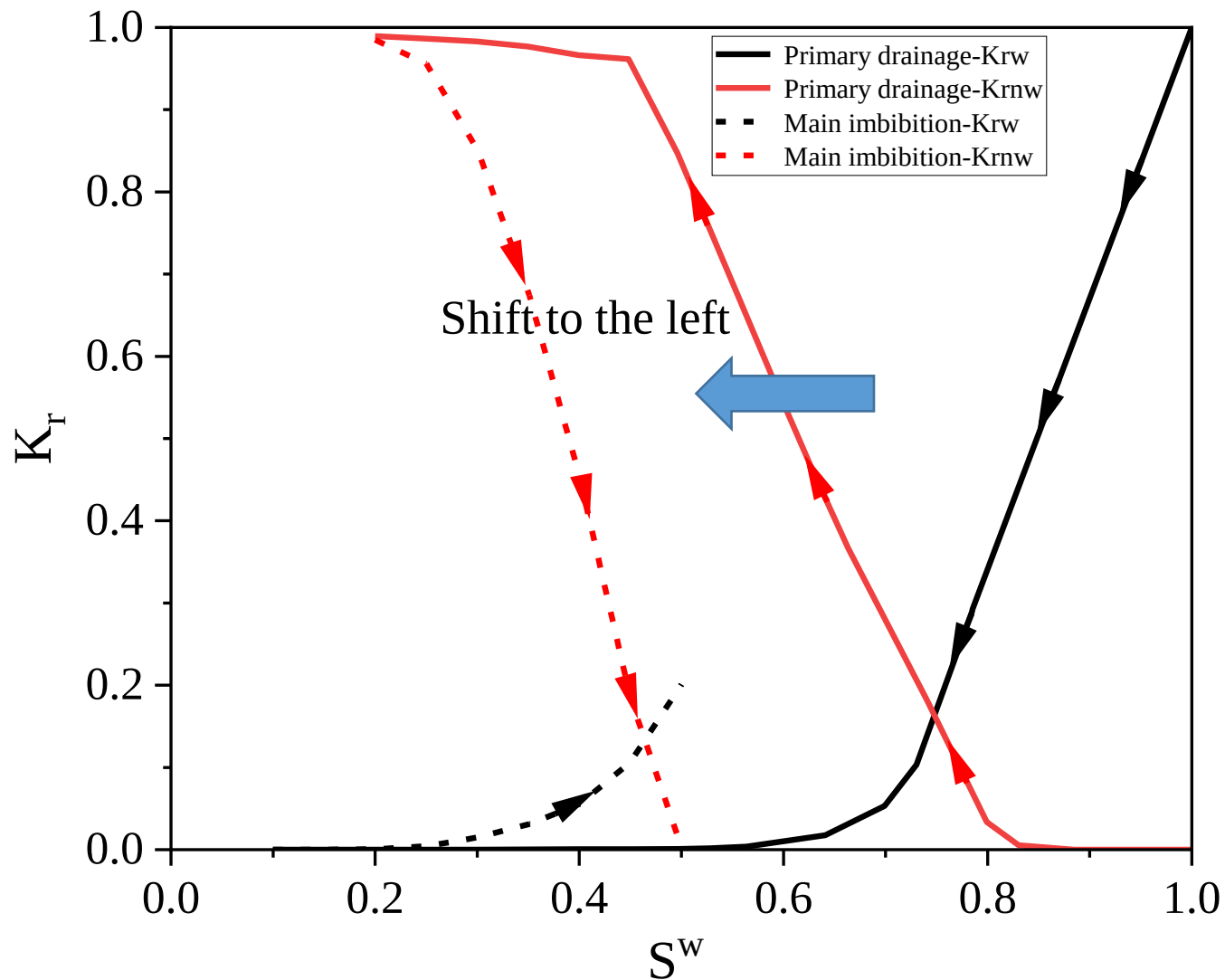
# Capillary pressure (the full image of ES6.5)



# Relative permeability (the full image of ES6.5)



# Relative permeability (the full image of ES6.5)



- 1. Introduction of multiscale pore-network model**
- 2. Predictions of absolute permeability and formation factor**
- 3. Predictions of capillary pressure and relative permeability**
- 4. Conclusions and outlook**



# Conclusions and outlook

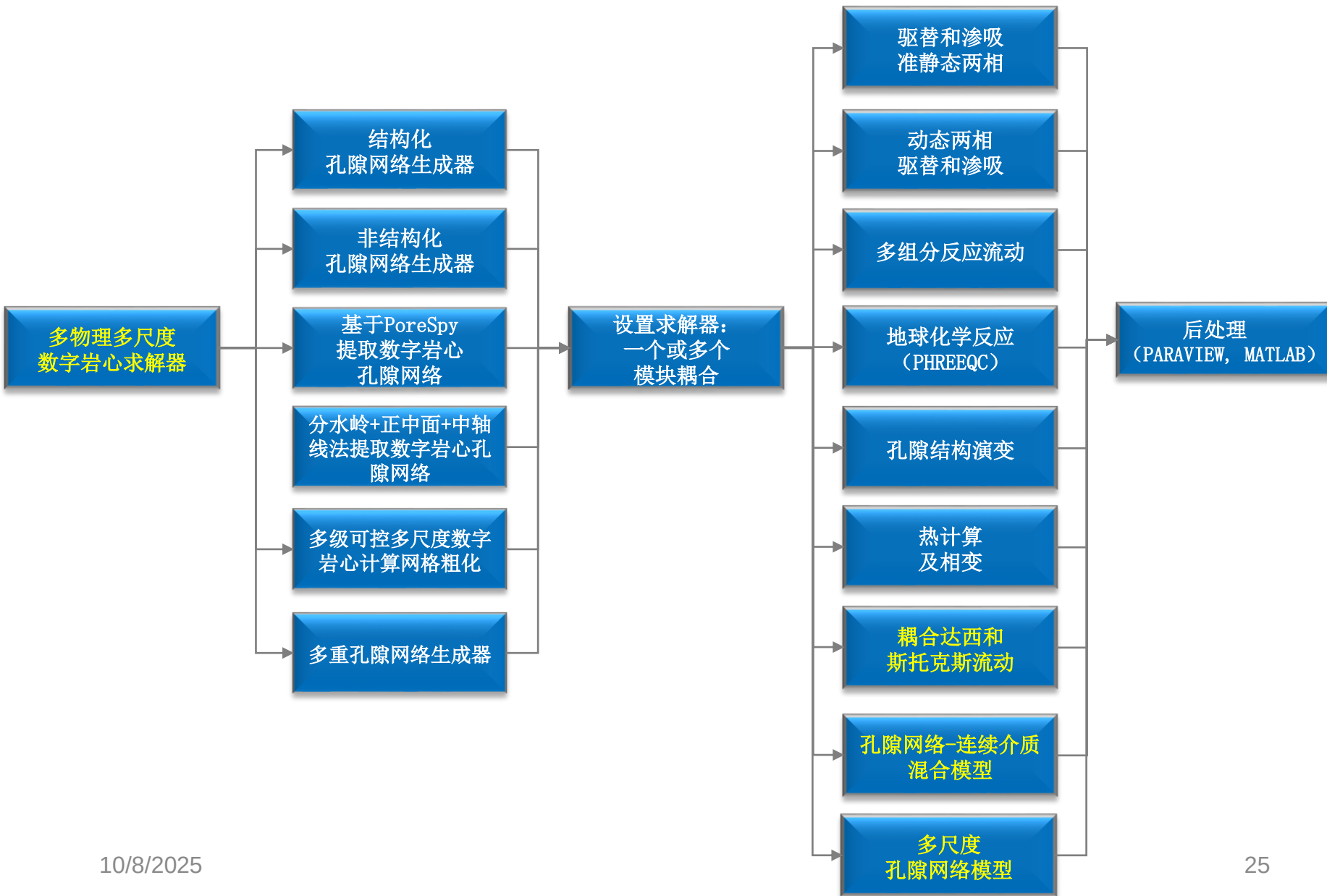
## Conclusions

- ❑ A **high-efficient** multiscale pore-network model (MPNM) is developed, and verified against the **high-resolution** pore-network-continuum model (PNCM).
- ❑ Microporosity of ES rocks has strong heterogeneity of mean pore sizes.
- ❑ Three types of averaging microporosity voxels are tested. It is found that **the sub-rock typing** is necessary to guarantee the reliable predictions of both single-phase and two-phase flow parameters.
- ❑ We can **well predict** absolute permeability, formation factor, capillary pressure and relative permeability.

## Outlook

- ❑ Advance the modeling framework to **two-phase flow dynamics**.
- ❑ Understand how microporosity influences material properties, and extend capillary pressure and relative permeability **empirical models**.
- ❑ **Seek for more applications and collaborations.**

# Multiphysics Multiscale Digital Rock Simulator (MMDRS)



# References

1. X. Zhao, B. Shi, X. Wang, J. Zhao, F. Jiang, C.Z. Qin. Modeling of permeability and formation factor of carbonate digital rocks: dual-pore-network and pore-network-continuum models. *Transport in Porous Media*, 152:37, 2025
2. B. Shi, H. Jiang, B. Guo, J. Tian, and C.Z. Qin. Modeling of flow and transport in multiscale digital rocks aided by grid coarsening of microporous domains. *Journal of Hydrology*, 633: 131003, 2024.
3. C.Z. Qin, H. van Brummelen, M. Hefny, and J. Zhao. Image-based modeling of spontaneous imbibition in porous media by a dynamic pore network model. *Advances in Water Resources*, 152: 103932, 2021.
4. L. Zhang, B. Guo, C.Z. Qin, Y. Xiong. A hybrid pore-network-continuum modeling framework for flow and transport in 3D digital images of porous media. *Advances in Water Resources*, 190: 104753, 2024.
5. H. Jiang, C. Arns, Y. Yuan, C.Z. Qin. SVM-based fast 3D pore-scale rock-typing and permeability upscaling for complex rocks using Minkowski functionals. *Advances in Water Resources*, 183: 104605, 2024.
6. C.Z. Qin, X. Wang, M. Hefny, J. Zhao, S. Chen, and B. Guo. Wetting dynamics of spontaneous imbibition in porous media: from pore scale to Darcy scale. *Geophysical Research Letters*, 49, e2021GL097269, 2022.

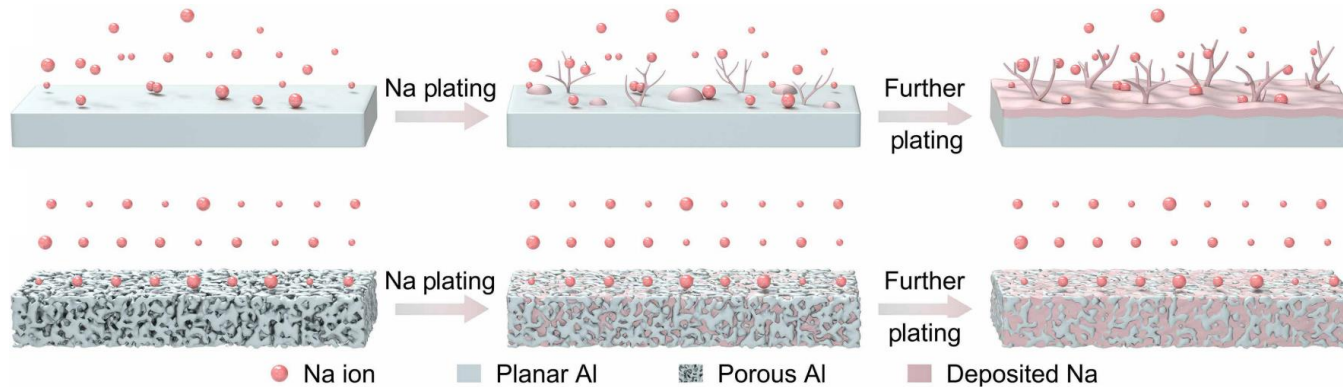


Thank you for  
your attention!



# Research challenges for flow and transport

## Reduce Na dendrites



## Design of porous anode current collectors

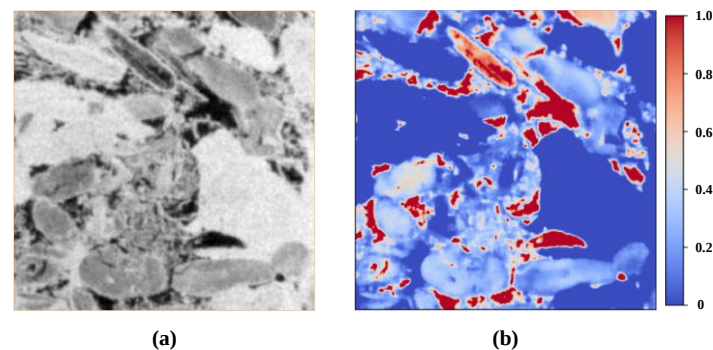
# Test samples of carbonate digital rocks

<https://www.digitalrockportal.org/>

| Digital rock | Voxel size (μm) | Microporosity          | Image size (voxels) | Total Porosity (%) | Absolute permeability (mD) |
|--------------|-----------------|------------------------|---------------------|--------------------|----------------------------|
|              |                 |                        |                     |                    | Experimental               |
| ES3.1        | 3.1             | Uniform mean pore size | 2000×2000×1725      | 25                 | 260 ± 60                   |
| ES3.6        | 3.6             | Uniform mean pore size | 1000×1000×1000      | 29                 | /                          |
| ES6.5        | 6.5             | Heterogeneous          | 1316×1316×1087      | 25                 | 202.4 ± 86.9               |

ES3.1 and ES3.6 have the MICP curves; ES6.5 has **the porosity map and the entry-pressure map** of subresolution microporosity.

The porosity map of ES6.5



# Predictions of absolute permeability and formation factor

| Subvolume of digital rock | Pore regions  | Original voxels | Volume fraction | In the MPNM | In the PNCM |
|---------------------------|---------------|-----------------|-----------------|-------------|-------------|
| ES3.1                     | Macropores    | 6332318         | 9.9%            | 3569        | 3569        |
|                           | Microporosity | 21562493        | 33.7%           | 8375        | 3929815     |
| ES3.6                     | Macropores    | 5040267         | 7.9%            | 2172        | 2172        |
|                           | Microporosity | 32676964        | 51.1%           | 13228       | 4494989     |
| ES6.5                     | Macropores    | 3694907         | 5.8%            | 3827        | 3827        |
|                           | Microporosity | 40618405        | 63.5%           | 7930        | 4147069     |

90%  
reduction in  
computational  
grids

Why does the MPNM  
underestimate the  
absolute permeability?

| Digital rock | Mean pore size (μm)         | By the MPNM (mD) | By the PNCM (mD) | By the reference model (mD) |
|--------------|-----------------------------|------------------|------------------|-----------------------------|
| ES3.1        | 0.61                        | 109              | 116              | 117                         |
| ES3.6        | 0.74                        | 34               | 37               | 37                          |
| ES6.5-1      | 1.81                        | 28               | 18               | 18                          |
| ES6.5-2      | Estimated by entry pressure | 12               | 128              | 174                         |

| Digital rock | By the multiscale pore-network model (-) | By the pore-network-continuum model (-) | By the reference model (-) |
|--------------|------------------------------------------|-----------------------------------------|----------------------------|
| ES3.1        | 17.24                                    | 19.61                                   | 19.23                      |
| ES3.6        | 23.81                                    | 23.81                                   | 23.26                      |
| ES6.5        | 18.52                                    | 20.41                                   | 19.23                      |

The prediction of  
formation factor is  
satisfied